



Tracer kinetics in the kidney with a two-compartment model

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Motivation Model-free analysis (perfusion)







Sourbron (2005) PhD thesis, VU Brussel Dujardin et al. (2005) *MRM* **54** 841



Motivation Model-free analysis (filtration)

<u>Male 53y (Healthy)</u> Serum creatinine 0.84 ml/100 ml Creatinine Clearance 57.6 ml/min *MRI-GFR 37.5 ml/min*



Male 54y (Under chemotherapy) Serum creatinine 1.8 ml/100 ml Creatinine Clearance 43 ml/min *MRI-GFR 22.7 ml/min*



Dujardin et al. (2005) ESMRMB Basel



Motivation Towards a modelling approach



Dujardin et al. (2005) ESMRMB Basel

Model-free filtration

- Weak correlation
- Justification?
- Subjective?

Modelling methods

- Clear interpretation
- User-independent
- Additional parameters



Motivation Some Context

1-compartment model ROI, rats (Baumann 2000) 2-compartment model Patlak ROI, humans (Hackstein 2003) ROI, rats (Pedersen 2004) Voxel, humans (Grenier 2006) Tofts ROI, humans (Buckley 2006) Separable ROI, rabbits (Annet 2004) Voxel, ROI, humans (...) 3-compartment model

ROI, humans (Hackstein 2003)



Theory A single compartment

















 $N(t) = C_{in}(t) * (F_e^{-t / T_-} + F_e^{-t / T_+})$





$$N(t) = C_{in}(t) * (F_{-}e^{-t / T_{-}} + F_{+}e^{-t / T_{+}})$$
$$\bigcup ?$$
$$F_{P}, F_{TP}, F_{PT}, T_{P}, T_{T}$$





 $N(t) = C_{in}(t) * (F_e^{-t / T_e} + F_e^{-t / T_e})$



4 parameter fit \rightarrow 5 parameter model !

$$F_{\rm P}$$
, $F_{\rm TP}$, $F_{\rm PT}$, $T_{\rm P}$, $T_{\rm T}$



Theory Separable 2-compartment model (single inlet)



Annet et al. (2004) with different terminology



 $N(t) = C_{in}(t) * F_{P} R_{P} (t)$ $+ C_{in}(t) * H_{P} (t) * F_{T} R_{T} (t)$



Theory Separable 2-compartment model (single inlet)

$$F_{\rm P} \longrightarrow T_{\rm P} \longrightarrow T_{\rm T} \longrightarrow$$

 $N(t) = C_{in}(t) * F_{P} e^{-t / T_{P}} + C_{in}(t) * T_{P}^{-1} e^{-t / T_{P}} * F_{T} e^{-t / T_{T}}$



Theory Separable 2-compartment model (single inlet)

$$F_{\rm P} \longrightarrow T_{\rm P} \longrightarrow T_{\rm T} \longrightarrow$$



Theory Common approximations

$$N(t) = C_{in}(t) * F_{P} e^{-t / T_{P}} + C_{in}(t) * T_{P}^{-1} e^{-t / T_{P}} * F_{T} e^{-t / T_{T}}$$

 $\int T_P \rightarrow 0, V_P = const$ ("Tofts" approximation)

 $N(t) = C_{in}(t) V_{P} + C_{in}(t) * F_{T} e^{-t / T_{T}}$



Theory Common approximations

$$N(t) = C_{in}(t) * F_{P} e^{-t / T_{P}} + C_{in}(t) * T_{P}^{-1} e^{-t / T_{P}} * F_{T} e^{-t / T_{T}}$$

 $\int T_P \rightarrow 0, V_P = const$ ("Tofts" approximation)

 $N(t) = C_{in}(t) V_{P} + C_{in}(t) * F_{T} e^{-t / T_{T}}$

 $\bigcup T_{T} \to \infty, F_{T} = const \quad ("Patlak" approximation)$

 $N(t) = C_{in}(t) V_{P} + C_{in}(t) * F_{T}$



Study objectives

Why approximate?

Or: Optimize and evaluate the separable 2compartment model for the quantification of filtration and perfusion in humans on ROI- and voxel level



Methods Measurement protocol

- MRI protocol
 - 1.5 T (Siemens Avanto)
 - 2D SR-TURBO-FLASH (TR 254ms, TE 1.04ms, FA 12°, Matrix 192x154)
 - 1 sec , 4 slices (1 axial, 3 coronal)
- 15 Volunteers
 - 7ml Gd-BOPTA (0.5 mM) at 4ml/sec (Multihance, Bracco-Altana)
 - Breath-hold for 60s + PACE triggering
- 1 Patient
 - Left renal artery stenosis
 - 7ml Gadobutrol (1.0 mM) at 4ml/sec (Gadovist, Schering)
 - Free-breathing + triggering on post-processing



Methods Post-processing

- Signal → Signal Enhancement
- Manual ROI selection
 - Aorta, Whole Kidney, Cortex
 - Manual motion correction!
- Tracer kinetic analysis
 - (1) Deconvolution
 - (2) Patlak 2-compartment model
 - Linear fit (40-110 sec after contrast arrival)
 - (3) Tofts + open 2-compartment models
 - Non-linear fit (all dynamics)
 - Fixed initial values (= literature values)



First Results 2 test-cases, no motion correction



First Results

Curve fits (volunteer)



Figure 1. A plot of the data (blue) and the fit provided by the model (red) for the cortex (left column) and the medulla (right column). The top row gives the result for the whole-ROI curves, the bottom row for an individual pixel inside the ROI. Values for the fitted model parameters are presented next to the curves. Flow values (PF and TF) are given in ml/100ml/min, volumes (PV and TV) in ml/100ml.



First Results

Pixel data (volunteer)





First Results

Pixel data (volunteer)









First Results Pixel data (patient)





First Results Comparison to deconvolution (volunteer)

Plasma Flow (ml/100ml/min)

2-compartment model



Deconvolution





First Results Comparison to Patlak (patient)

Patlak

20 -40 5.6 1.8 12 15 -30 **Tubular Flow** -2010(ml/100ml/min) -5 -100 -0 ·40 -40 19 21 28 28 ·30 -30 Plasma Volume (ml/100ml) 20-20-10 -10

2-compartment model

-0



First Results Temporal constraints (volunteer)





Results 15 volunteers



ROI data (15 volunteers)







ROI data (15 volunteers)

1 Doromotor fit	KIDNEY		CORTEX	
4-ralameter m	Mean	Stddev	Mean	Stddev
Plasma Flow (ml/100ml/min)	229	57	340	86
Plasma Volume (ml/100ml)	24	3.4	36	4.7
Tubular Flow (ml/100ml/min)	15	3.6	10	5.4
Tubular Volume (ml/100ml)	31	12	19	7.7
Plasma Mean Transit Time (sec)	6.5	1.3	6.6	1.2
Tubular Mean Transit Time (sec)	125	55	123	62
Root-Mean-Square Error (%)	0.5	0.2	0.8	0.8

Table 1: Mean and standard deviations of the fitted model parameters and therelative root-mean-square error of the fit. The mean transit times of bothcompartments can be obtained from the four fit parameters using the centralvolume theorem.

Note: "Typical" values

- *TF*: (120 ml/min) / 400g = 30 ml/min/100g
- *PF*: 220-275 ml/100g/min (cortex)
- PV: 15 ml/100g (cortex)
- PT: 3-5 sec (capillary bed)
- *TT*: 1-3 min









PV (0-40ml/100ml)











Cortex ROI	PF (ml/100ml/min)	PV (ml/100ml)	TF (ml/100ml/min)	TV (ml/100ml)
ROI analysis	309 (45)	35 (4.0)	11 (5.3)	21 (6.5)
Pixel Analysis	309 (43)	35 (4.2)	11 (5.3)	21 (7.1)



Results Comparison of methods (15 volunteers)

Kidney ROI	PF (ml/100ml/min)	PV (ml/100ml)	TF (ml/100ml/min)	TV (ml/100ml)	Chi-Square (%)
4-Parameter model	229 (57)	24 (3.4)	15 (3.6)	31 (12)	0.47 (0.23)
5-Parameter model	337 (68)	22 (3.3)	18 (4.8)	33 (11)	0.29 (0.14)
Deconvolution / Patlak	210 (50)	24 (6.2)	12 (3.2)	30 (8.7)	N/A

Note: Arterial delay 1.5s (0.5s)

Cortex ROI	PF (ml/100ml/min)	PV (ml/100ml)	TF (ml/100ml/min)	TV (ml/100ml)	Chi-Square (%)
4-Parameter model	340 (86)	36 (4.7)	10 (5.4)	19 (7.7)	0.80 (0.83)
5-Parameter model	496 (136)	33 (4.6)	15 (7.8)	23 (5.8)	0.39 (0.19)
Deconvolution / Patlak	331 (70)	38 (10)	7.3 (5.5)	18 (8.5)	N/A

Note: Arterial delay 1.4s (0.5s)



Results Comparison to Tofts model (15 volunteers)



Figure 1. A plot of the data and both model fits for the first 60 sec in a typical case. Note that the arterial peak in the Tofts-fit is narrower than that of the General model since the Tofts model does not allow for intravascular dispersion. The fits in later phases of the contrast passage (>1min) show no obvious differences.

Fitted Parameters		KIDNEY		CORTEX	
		Mean	Stddev	Mean	Stddev
PV	General Model	24	3.4	36	4.7
	Tofts Model	17	2.8	24	4.2
	Patlak	24	6.2	38	10
TF	General Model	15	3.6	10	5.4
	Tofts Model	28	8.3	49	40
	Patlak	12	3.2	7.3	5.5
Π	General Model	125	53	123	60
	Tofts Model	84	37	48	19
RMS	General Model	0.5	0.2	0.8	0.8
	Tofts Model	0.8	0.7	0.9	0.3

Table 1. Values of the fitted parameters Plasma Volume (ml/100ml), Tubular Flow (ml/100ml/min) and Tubular Mean Transit Time (sec). The bottom two rows give the relative Root-Mean-Square error of the fit (%). The values in red are significantly different from those obtained with the Patlak model.

4-parameter Tofts model versus 4-parameter separable model



Results Temporal constraints (15 volunteers)





Future research

- Motion correction!!
 - Acquisition (3D?)
 - Post-processing
 - Retrospective triggering
 - Deformable registration
- Improve robustness with hybrid methods?
 - Initial values from deconvolution/Patlak
 - Fix selected parameters to deconvolution/Patlak values
- Signal optimization & Dynamic T1quantification
- Clinical evaluation



Thank you!